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IDENTIFICATION OF OPTIMAL WASTEWATER SYSTEM PARAMETERS AIMED AT MAXIMIZING ECONOMIC PERFORMANCE

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Abstract: In this article, a selection procedure for identifying the most influential parameters of a wastewater treatment system with respect to maximizing economic profit is presented. Optimal wastewater treatment configurations require the adjustment of numerous system parameters to obtain economically efficient solutions. Such optimal solutions are commonly defined in terms of maximizing economic performance, typically expressed through minimizing the total cost of the wastewater treatment system. However, applying classical analytical optimization methods to this problem is time-consuming and computationally demanding due to the system's high degree of nonlinearity. Accordingly, the primary objective of this study was to determine which parameters of the wastewater treatment system exert the greatest influence on overall economic profit. To support this selection process, an Adaptive Neuro-Fuzzy Inference System (ANFIS) was employed, as this method is well-suited for handling nonlinear relationships and redundant datasets. The results indicate that system size is the dominant factor affecting economic outcomes. The obtained findings have practical significance, as they provide guidance for selecting the most economically favorable configuration for a given wastewater treatment system.

Keywords: Wastewater, Economic profit, Optimal solution, ANFIS.

INTRODUCTION

Wastewater treatment systems are inherently complex, comprising numerous interdependent parameters that influence overall process performance. To achieve substantial economic benefits in rural wastewater treatment applications, it is essential to identify those parameters that exert the greatest impact on economic profit. These key parameters simultaneously represent the primary contributors to the total costs of the wastewater treatment system. Consequently, economic profit is typically evaluated through the minimization of total system costs.

The selection of an optimal solution is of critical importance when applying economic criteria to wastewater treatment system design and operation (Abdelf-Fatah, 2018). Research on the sustainable development of wastewater systems consistently highlights the necessity of integrating environmental, social, and economic dimensions within the decision-making process (Ansari et al., 2019). Various technological configurations have been investigated to enhance wastewater treatment performance. For example, two

technological setups were analyzed in (Jokanović et al., 2017), forming the basis for four alternative wastewater reclamation scenarios. In another study, a sequential approach to hydrogen and methane production from dairy industry wastewater was explored using *Enterobacter aerogens* and methanogenic bacteria derived from cow dung, demonstrating simultaneous pollutant reduction and biofuel generation (Novković-Cvetković et al., 2019). A thermo-economic analysis of hybrid solar conventional energy supply in a zero-liquid-discharge plant was presented in (Elreedy et al., 2019), while biogas production through anaerobic digestion of organic waste and manure has shown potential to reduce greenhouse gas emissions across multiple sectors, including waste management, transportation, energy, and agriculture (Deneva et al., 2017).

Further investigations include the development of a wastewater metabolism input–output model aimed at providing a novel framework for sustainable industrial wastewater flow assessment among economic sectors (Kothari et al., 2017). Advances in nanofiltration membrane (NF) technologies continue to represent a crucial component within modern wastewater treatment processes (Lyng et al., 2018). Additionally, independent hydrogen production from petrochemical wastewater containing mono-ethylene glycol (MEG) has been comprehensively evaluated under psychrophilic conditions using an anaerobic sequencing batch reactor (ASBR) (Mladenovic et al., 2016). Domestic wastewater, owing to its high nutrient content, also offers substantial potential for nutrient recovery through dedicated wastewater treatment technologies (Nikolić et al., 2018).

Classical analytical optimization approaches applied to wastewater treatment systems require considerable time and computational effort due to the pronounced nonlinearity of the governing equations. Therefore, the principal objective of this study is to identify the parameters of a wastewater treatment system that have the most significant influence on its economic profitability. To facilitate this selection process, an Adaptive Neuro-Fuzzy Inference System (ANFIS) was employed (Murashko et al., 2018; Najafi et al., 2019; Padilla-Rivera and Güereca, 2019; Nikolić et al., 2018; Zheng et al., 2019), as this method is particularly suitable for handling nonlinear, redundant, and complex datasets.

MATERIAL AND METHODS

Database of Wastewater System

To implement the ANFIS model, it was necessary to prepare a comprehensive database consisting of input-output data samples. Table 1 presents all variables used in the study. The input parameters include: system size; elongation factor (i.e., the length-to-width ratio of the settlement); dispersion factor (defined as the ratio between the number of households and the sewer network length); vertical terrain uniformity; proximity to the urban centre (distance between the settlement and the nearest urban node); degree of settlement clustering (distance between neighboring settlements); and distance between the wastewater treatment plant and the settlement. The total construction cost of the wastewater treatment system was used as the output variable.

Table 1. Input and output parameters of the wastewater system

| Input 1 Size | Input 2 Elongation | Input 3 Dispersion | Input 4 Uniformity | Input 5 Vicinity | Input 6 Grouping | Input 7 Distance | Output Total costs |
|-----------------|-----------------------|-----------------------|-----------------------|---------------------|---------------------|---------------------|-----------------------|
| 284.9 | 3 | 0.02 | 4.96 | 6.01 | 1.17 | 0.96 | 1039705.4 |

ANFIS Methodology

ANFIS network has five layers as it shown in Figure 1. The main core of the ANFIS network is fuzzy inference system. Layer 1 receives the inputs and convert them in the fuzzy value by membership functions. In this study bell shaped membership function is used since the function has the highest capability for the regression of the nonlinear data.



Figure 1. ANFIS layers

Bell-shaped membership function is defined as follows:

$$\mu(x) = bell(x; a_i, b_i, c_i) = \frac{1}{1 + \left[\frac{(x - c_i)}{a_i} \right]^{2b_i}} \quad (1)$$

where $\{a_i, b_i, c_i\}$ is the parameters set and x is input.

Second layer multiplies the fuzzy signals from the first layer and provides the firing strength of as rule. The third layer is the rule layers where all signals from the second layer are normalized. The fourth layer provides the inference of rules, and all signals are converted in crisp values. The final layers summarized all signals and provided the output crisp value.

RESULTS AND DISCUSSION

Accuracy Indices

Performances of the proposed models are presented as root means square error (RMSE), Coefficient of determination (R^2) and Pearson coefficient (r) as follows:

1) RMSE

$$RMSE = \sqrt{\frac{\sum_{i=1}^n (P_i - O_i)^2}{n}}, \quad (2)$$

2) Pearson correlation coefficient (r)

$$r = \frac{n \left(\sum_{i=1}^n O_i \cdot P_i \right) - \left(\sum_{i=1}^n O_i \right) \cdot \left(\sum_{i=1}^n P_i \right)}{\sqrt{\left(n \sum_{i=1}^n O_i^2 - \left(\sum_{i=1}^n O_i \right)^2 \right) \cdot \left(n \sum_{i=1}^n P_i^2 - \left(\sum_{i=1}^n P_i \right)^2 \right)}} \quad (3)$$

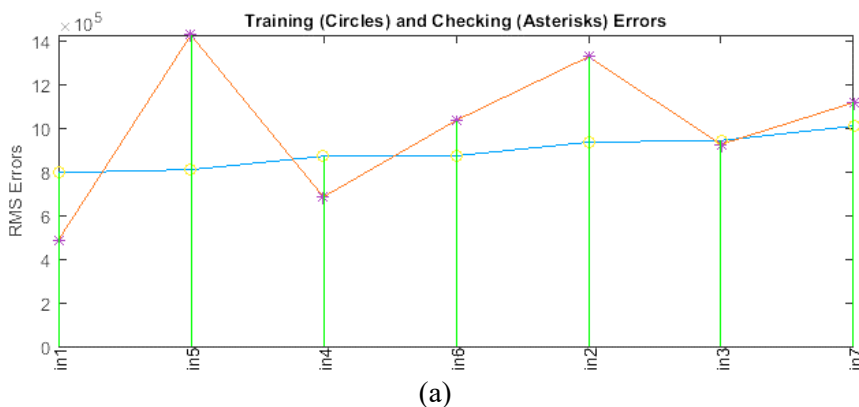
3) Coefficient of determination (R^2)

$$R^2 = \frac{\left[\sum_{i=1}^n (O_i - \bar{O}_i) \cdot (P_i - \bar{P}_i) \right]^2}{\sum_{i=1}^n (O_i - \bar{O}_i)^2 \cdot \sum_{i=1}^n (P_i - \bar{P}_i)^2} \quad (4)$$

where P_i and O_i are known as the experimental and forecast values, respectively, and n is the total number of datasets.

ANFIS Results

Table 3 shows the prediction errors for the total costs or economic profit of the wastewater system for single, two and three input parameters. Training RMSE shows influence of the inputs for the wastewater total costs. Smaller training errors have more influence on the wastewater total costs. Checking RMSE is used for overfitting tracking between training and checking data. Here one can see there is small overfitting for two and three input combinations since checking errors do not track training errors very well. As can be seen for single input parameters influence in Figure 2a the input parameters system size has the smallest training error therefore largest influence on the total costs of the wastewater system. Figure 2b shows two parameters' combinations and their corresponding training and checking errors for the total costs prediction of the wastewater system where combination of vicinity and distance has the smallest training error, hence the largest impact on the economic profit of the wastewater system. Finally Figure 2c shows three input combinations where one can see that the parameter system size, dispersion and vicinity form the optimal combination of three parameters for the total costs prediction of the wastewater system. Tables 2-4 show the numerical training and checking errors for all inputs combinations of the total costs prediction of the wastewater system where bolded values represent the optimal combinations.



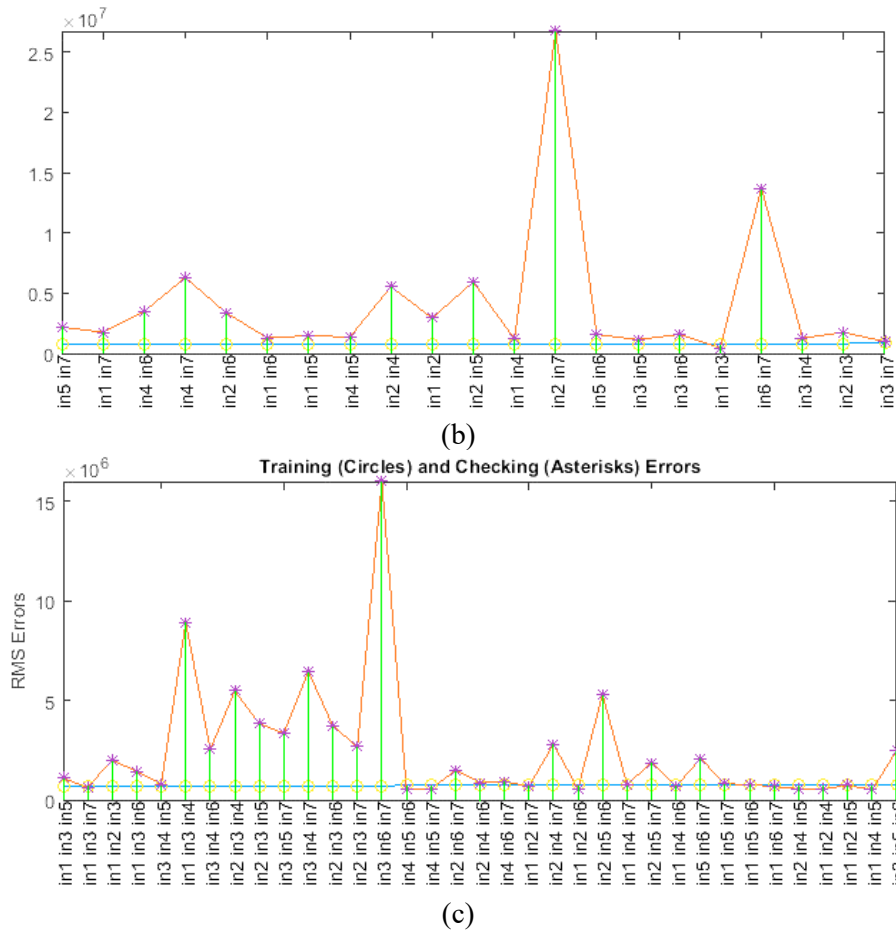


Figure 2. Inputs' influence on the output: (a) single inputs, (b) two inputs, (c) three inputs

Table 2. Single inputs' influence on the output

| | |
|--|------------------------|
| ANFIS model 1: in1 --> trn=795052.3800 | chk=486121.6677 |
| ANFIS model 2: in2 --> trn=934493.0105 | chk=1325577.0070 |
| ANFIS model 3: in3 --> trn=942358.2941 | chk=924852.5804 |
| ANFIS model 4: in4 --> trn=870057.7917 | chk=684031.8942 |
| ANFIS model 5: in5 --> trn=809001.7197 | chk=1425160.2330 |
| ANFIS model 6: in6 --> trn=872226.5836 | chk=1033930.6644 |
| ANFIS model 7: in7 --> trn=1008353.1837 | chk=1116116.8827 |

Table 3. Two inputs' influence on the output

| | |
|---|------------------|
| ANFIS model 1: in1 in2 --> trn=724825.7907 | chk=2931102.1642 |
| ANFIS model 2: in1 in3 --> trn=774927.9722 | chk=462781.9739 |
| ANFIS model 3: in1 in4 --> trn=724825.9920 | chk=1199555.0113 |
| ANFIS model 4: in1 in5 --> trn=724825.7715 | chk=1471737.5135 |
| ANFIS model 5: in1 in6 --> trn=721190.5829 | chk=1284921.6765 |
| ANFIS model 6: in1 in7 --> trn=721190.0175 | chk=1756868.7562 |
| ANFIS model 7: in2 in3 --> trn=813386.0264 | chk=1746867.8528 |
| ANFIS model 8: in2 in4 --> trn=724825.7716 | chk=5531286.3668 |
| ANFIS model 9: in2 in5 --> trn=724825.8296 | chk=5920287.0186 |
| ANFIS model 10: in2 in6 --> trn=721190.1054 | chk=3351655.9556 |

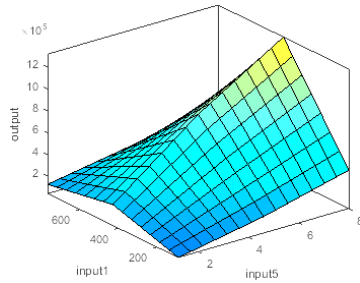
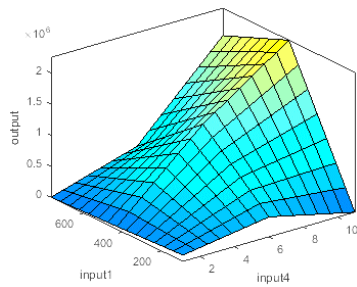
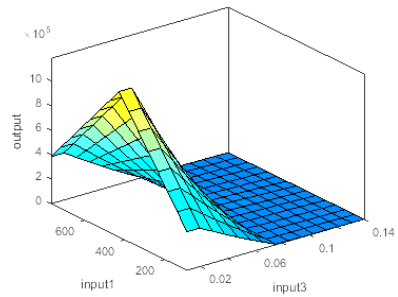
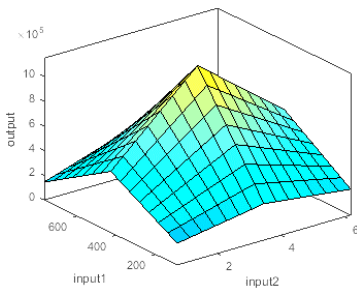
| | | |
|---------------------------------------|------------------------|-------------------------|
| ANFIS model 11: in2 in7 --> | trn=732752.1817 | chk=26719811.3762 |
| ANFIS model 12: in3 in4 --> | trn=791683.6982 | chk=1265159.0159 |
| ANFIS model 13: in3 in5 --> | trn=762214.7836 | chk=1137596.5035 |
| ANFIS model 14: in3 in6 --> | trn=772622.1657 | chk=1570964.2008 |
| ANFIS model 15: in3 in7 --> | trn=873703.5481 | chk=975834.5975 |
| ANFIS model 16: in4 in5 --> | trn=724825.7715 | chk=1362411.5779 |
| ANFIS model 17: in4 in6 --> | trn=721190.0175 | chk=3462676.9435 |
| ANFIS model 18: in4 in7 --> | trn=721190.1050 | chk=6293597.5250 |
| ANFIS model 19: in5 in6 --> | trn=756651.3649 | chk=1562383.1620 |
| ANFIS model 20: in5 in7 --> | trn=721190.0066 | chk=2184588.3894 |
| ANFIS model 21: in6 in7 --> | trn=788304.2828 | chk=13688525.4462 |

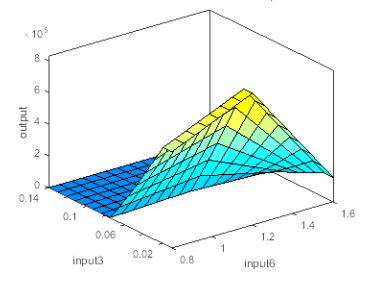
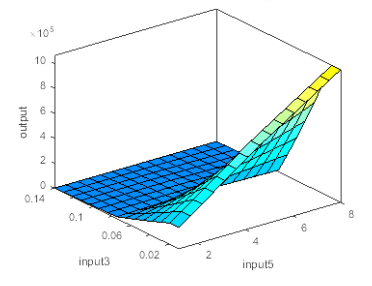
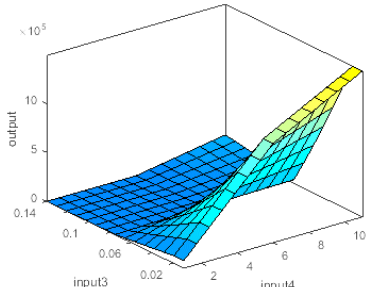
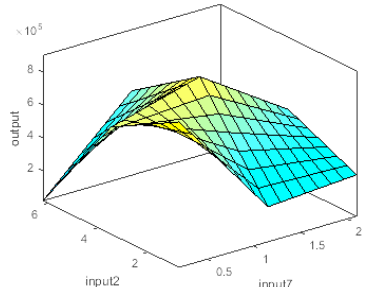
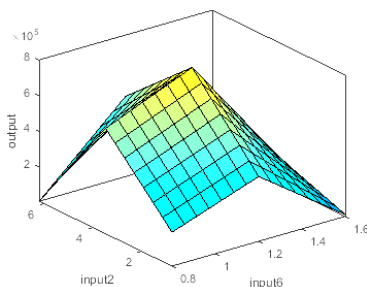
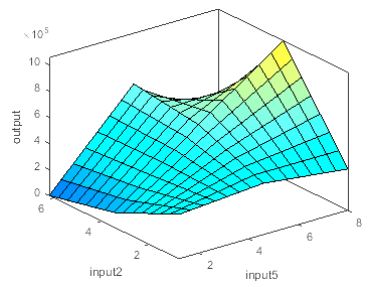
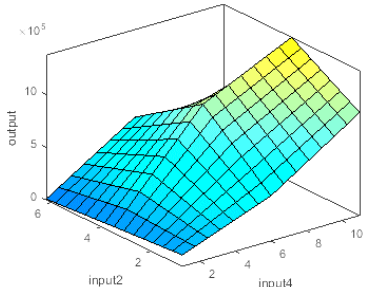
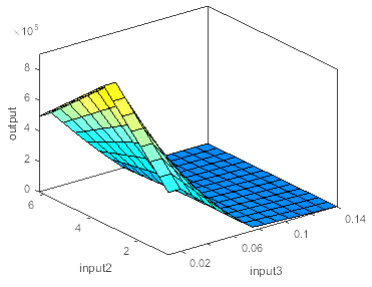
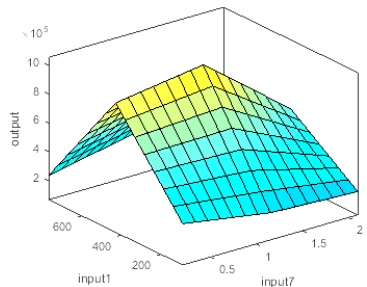
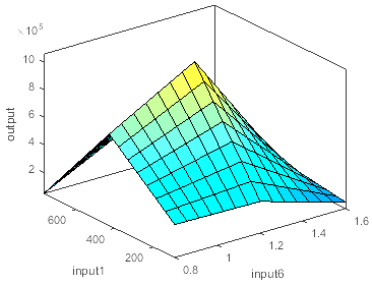
Table 4. Three inputs' influence on the output

| | | |
|--|------------------------|-------------------------|
| ANFIS model 1: in1 in2 in3 --> | trn=717062.3526, | chk=1991830.1402 |
| ANFIS model 2: in1 in2 in4 --> | trn=724825.7715 | chk=541577.8279 |
| ANFIS model 3: in1 in2 in5 --> | trn=724825.7719 | chk=727232.1725 |
| ANFIS model 4: in1 in2 in6 --> | trn=721190.0012 | chk=550695.9397 |
| ANFIS model 5: in1 in2 in7 --> | trn=721190.0012 | chk=676052.4503 |
| ANFIS model 6: in1 in3 in4 --> | trn=717062.3621 | chk=8919082.8974 |
| ANFIS model 7: in1 in3 in5 --> | trn=717062.3524 | chk=1080947.4127 |
| ANFIS model 8: in1 in3 in6 --> | trn=717062.3528 | chk=1437260.3746 |
| ANFIS model 9: in1 in3 in7 --> | trn=717062.3526 | chk=642086.9245 |
| ANFIS model 10: in1 in4 in5 --> | trn=724825.7729 | chk=515033.0225 |
| ANFIS model 11: in1 in4 in6 --> | trn=721190.0012 | chk=673446.7701 |
| ANFIS model 12: in1 in4 in7 --> | trn=721190.0012 | chk=774892.2500 |
| ANFIS model 13: in1 in5 in6 --> | trn=721190.0068 | chk=780201.7730 |
| ANFIS model 14: in1 in5 in7 --> | trn=721190.0028 | chk=799408.8123 |
| ANFIS model 15: in1 in6 in7 --> | trn=721190.0161 | chk=667044.1730 |
| ANFIS model 16: in2 in3 in4 --> | trn=717062.3679 | chk=5470009.1720 |
| ANFIS model 17: in2 in3 in5 --> | trn=717062.3735 | chk=3823271.6177 |
| ANFIS model 18: in2 in3 in6 --> | trn=717062.5549 | chk=3718324.6971 |
| ANFIS model 19: in2 in3 in7 --> | trn=717063.6139 | chk=2667008.2019 |
| ANFIS model 20: in2 in4 in5 --> | trn=724825.7714 | chk=563687.6772 |
| ANFIS model 21: in2 in4 in6 --> | trn=721190.0012 | chk=861955.0153 |
| ANFIS model 22: in2 in4 in7 --> | trn=721190.0012 | chk=2797595.2049 |
| ANFIS model 23: in2 in5 in6 --> | trn=721190.0012 | chk=5292965.2192 |
| ANFIS model 24: in2 in5 in7 --> | trn=721190.0012 | chk=1869850.4545 |
| ANFIS model 25: in2 in6 in7 --> | trn=721190.0012 | chk=1486697.1116 |
| ANFIS model 26: in3 in4 in5 --> | trn=717062.3536 | chk=779282.7756 |
| ANFIS model 27: in3 in4 in6 --> | trn=717062.3626 | chk=2528292.0317 |
| ANFIS model 28: in3 in4 in7 --> | trn=717062.4691 | chk=6453906.4347 |
| ANFIS model 29: in3 in5 in6 --> | trn=730327.4828 | chk=2471711.0046 |
| ANFIS model 30: in3 in5 in7 --> | trn=717062.3805 | chk=3332526.6893 |
| ANFIS model 31: in3 in6 in7 --> | trn=717679.4983 | chk=15975926.5099 |
| ANFIS model 32: in4 in5 in6 --> | trn=721190.0012 | chk=539168.0373 |
| ANFIS model 33: in4 in5 in7 --> | trn=721190.0012 | chk=548010.1157 |
| ANFIS model 34: in4 in6 in7 --> | trn=721190.0012 | chk=925331.3952 |
| ANFIS model 35: in5 in6 in7 --> | trn=721190.0023 | chk=2079240.9627 |

Figure 3 shows the ANFIS decision surfaces for the economic profit of wastewater treatment system based on different combinations of inputs. The combinations created based on mean values of the inputs and can be listed as follows:

-
1. *Input 1* *Input 2* 0.02616 4.964 6.015 1.178 0.9673
 2. *Input 1* 3.008 *Input 3* 4.964 6.015 1.178 0.9673
 3. *Input 1* 3.008 0.02616 *Input 4* 6.015 1.178 0.9673
 4. *Input 1* 3.008 0.02616 4.964 *Input 5* 1.178 0.9673
 5. *Input 1* 3.008 0.02616 4.964 6.015 *Input 6* 0.9673
 6. *Input 1* 3.008 0.02616 4.964 6.015 1.178 *Input 7*
 7. 284.9 *Input 2* *Input 3* 4.964 6.015 1.178 0.9673
 8. 284.9 *Input 2* 0.02616 *Input 4* 6.015 1.178 0.9673
 9. 284.9 *Input 2* 0.02616 4.964 *Input 5* 1.178 0.9673
 10. 284.9 *Input 2* 0.02616 4.964 6.015 *Input 6* 0.9673
 11. 284.9 *Input 2* 0.02616 4.964 6.015 1.178 *Input 7*
 12. 284.9 3.008 *Input 3* *Input 4* 6.015 1.178 0.9673
 13. 284.9 3.008 *Input 3* 4.964 *Input 5* 1.178 0.9673
 14. 284.9 3.008 *Input 3* 4.964 6.015 *Input 6* 0.9673
 15. 284.9 3.008 *Input 3* 4.964 6.015 1.178 *Input 7*
 16. 284.9 3.008 0.02616 *Input 4* *Input 5* 1.178 0.9673
 17. 284.9 3.008 0.02616 *Input 4* 6.015 *Input 6* 0.9673
 18. 284.9 3.008 0.02616 *Input 4* 6.015 1.178 *Input 7*
 19. 284.9 3.008 0.02616 4.964 *Input 5* *Input 6* 0.9673
 20. 284.9 3.008 0.02616 4.964 *Input 5* 1.178 *Input 7*
 21. 284.9 3.008 0.02616 4.964 6.015 *Input 6* *Input 7*
-





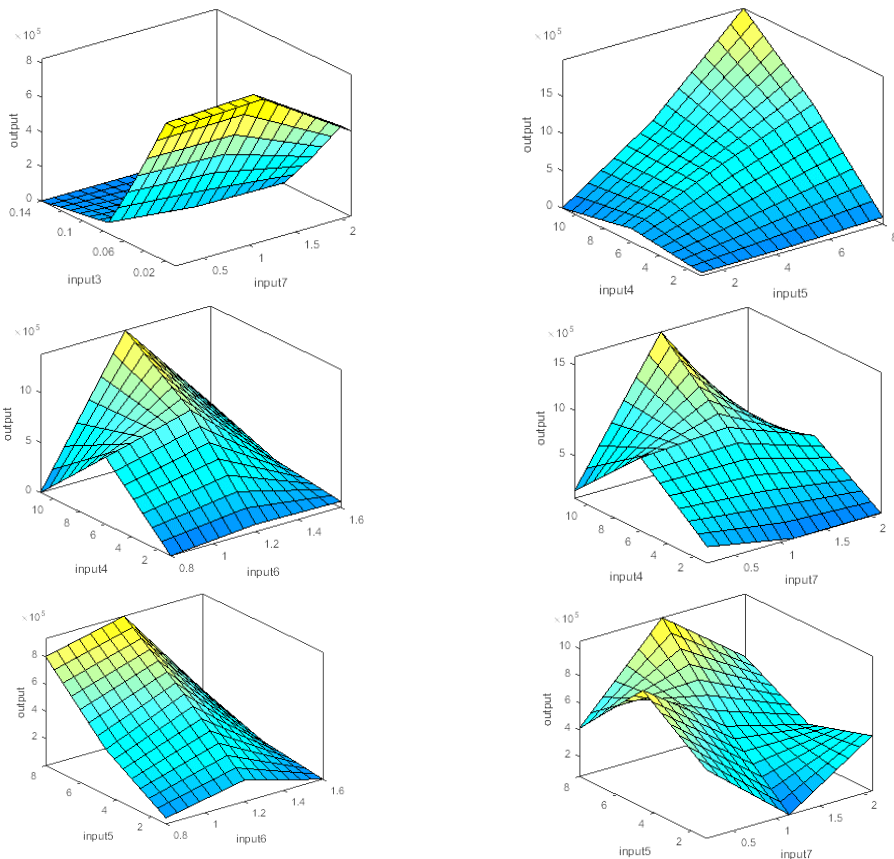


Figure 3. ANFIS decision surfaces for the economic profit of wastewater treatment system based on different combinations of inputs

CONCLUSION

In this article, adaptive neuro fuzzy inference system (ANFIS) is used for selection procedures in order to identify the most influential parameters of wastewater treatment system based on economic profit. Results revealed that the size of the system has the most influence on economic profit. Furthermore, obtained solutions could be of practical importance since one could select which solutions are the most suitable for particular wastewater treatment system.

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